



MURANG'A UNIVERSITY COLLEGE

(A Constituent college of Jomo Kenyatta University of Agriculture and Technology)

SEM 1302 ENGINEERING MATHEMATICS V1

DATE: 9TH DECEMBER, 2015

TIME:

INSTRUCTIONS:

Answer question **ONE** and **ANY** other **TWO** questions.

QUESTION ONE(30MKS):COMPULSORY

a) Define the following terms:

- i. Ordinary differential equation. (1mk)
- ii. Partial differential equation. (1mk)

b) State the order and the degree of the following differential equations:

- i. $\left(\frac{d^2y}{dx^2}\right)^3 + \frac{dy}{dx} = \sin x$ (2mks)
- ii. $\left(\frac{d^3y}{dx^3}\right)^{\frac{1}{2}} = k \frac{d^2y}{dx^2}$ (2mks)

c) Show that the function $f(x,y) = x^2 - y^2 + 2y$ is harmonic function. (3mks)

d) Find the complete general solution of the following equation:

$$\frac{d^2y}{dx^2} - 5 \frac{dy}{dx} + 6 = 0 \quad (3mks)$$

e) Evaluate $L^{-1} \left[\frac{2s+1}{s^3-4s} \right]$ (5mks)

f) Show that the equation $(3x^2 + 4xy)dx + (2x^2 + 2y)dy = 0$ is an exact differential equation. (2mks)

Hence solve the equation. (3mks)

g) Solve the following homogeneous differential equations of the first order.

$$(x^2 - y^2) \frac{dy}{dx} = 2xy \quad (4\text{mks})$$

h) Evaluate

$$L[t^2 e^{3t}] \quad (4\text{mks})$$

QUESTION TWO(20mks)

a) Solve the following homogeneous equation of first order

$$(x^2 - 3y^2)dx + 2xydy = 0 \quad (5\text{mks})$$

b) Solve the following differential equation by the method of separation of the variables

$$\frac{dy}{dx} = \frac{xy^2+x}{yx^2+y} \quad (5\text{mks})$$

c) Calculate the complete solution of the following differential equation:

$$\frac{d^2y}{dx^2} - 4 \frac{dy}{dx} + 4y = 0 \quad (5\text{mks})$$

d) Evaluate $L^{-1} \left[\frac{3s+1}{s^2+4s+13} \right]$ (5mks)

QUESTION THREE(20mks)

a) Let $f(z) = 2z^2 + 3z + 5i + 6$ be analytic. Show that the real and imaginary parts of $f(z)$ are harmonic. (5mks)

b) Show that the equation $(2xy + 1)dx + (x^2 + 4y)dy = 0$ is exact.
Hence, solve the equation. (5mks)

c) Solve the first order linear differential below using the method of integrating factor.

$$x \frac{dy}{dx} = y + x^3 + 3x^2 - 2x \quad (5\text{mks})$$

d) Solve the following homogeneous differential equations of the first order.

$$xy \frac{dy}{dx} = 3x^2 + xy \quad (5\text{mks})$$

QUESTION FOUR(20mks)

a) Solve the first order linear differential below using the method of integrating factor.

$$\frac{dy}{dx} = y \tan x - \sec x \quad (5\text{mks})$$

b) Solve the following Bernoulli's equation.

$$\frac{dy}{dx} - y = 4y^5 \quad (5\text{mks})$$

c) Use the method of undetermined coefficients to solve

$$y'' - 2y' - 3y = 3t^2 + 4t - 5 \quad (6\text{mks})$$

d) Evaluate $L[e^{2t} \sin 3t]$ (4mks)

QUESTION FIVE (20mks)

a) Solve the following Bernoulli equation:

$$\frac{dy}{dx} + y = xy^3 \quad (7\text{mks})$$

b) Prove that the transformation of $f(x, y) = x^2 - y^2 + 2y$ is also harmonic under the transformation $z = w^3$. (3mks)

c) Evaluate:

$$y \frac{dy}{dx} = 2x + y \quad (5\text{mks})$$

d) Evaluate:

$$L^{-1} \left[\frac{2s+4}{s^2-6s+25} \right] \quad (5\text{mks})$$