



## MURANG'A UNIVERSITY COLLEGE

(A Constituent College of Jomo Kenyatta University of Agriculture and Technology)

University Examination 2014/2015

Special/Supplementary Examination for the Diploma in Mechanical Engineering

SEM 1207: ENGINEERING MATHEMATICS IV

Date: October 2015

2 Hours

Instructions: Attempt Question **One** and any other **Two** Questions.

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### Question One (30 Marks)

a) Given the matrices

$$A = \begin{pmatrix} 1 & 3 \\ -5 & 2 \\ 0 & 6 \end{pmatrix} \text{ and } B = \begin{pmatrix} 3 & -4 & -2 \\ 1 & 2 & 7 \end{pmatrix}$$

show that AB is a singular matrix

(5 Marks)

b) Given the two matrices

$$A = \begin{pmatrix} 1 & 0 & 5 \\ 2 & -1 & 4 \\ 3 & -2 & 1 \end{pmatrix} \text{ and } B = \begin{pmatrix} 7 & -10 & 5 \\ 10 & -14 & 6 \\ -1 & 2 & -1 \end{pmatrix}$$

Find the matrix product AB hence determine  $A^{-1}$

(4 Marks)

c) Obtain the first three non-zero terms of the Maclaurin's series expansion for

$$f(x) = \sinh(x)$$

(5 Marks)

d) Given the function  $f(x) = 2x + 3$ , find  $f^{-1}(x)$  hence verify that  $(f \circ f^{-1})(x) = x$

(5 Marks)

e) Evaluate  $\text{Sinh}(3 + 5j)$

(6 Marks)

f) Express  $\tanh^{-1}(x - 2)$  in terms of logarithms

(5 Marks)

### Question Two (20 Marks)

a) Obtain the first 4 non-zero terms of the Taylor's series expansion for  $f(x) = \ln(x)$  about  $x = 1$

(5 Marks)

b) Find the values of  $x$  that satisfy the equation  $\cosh(x) - 5\sinh(x) - 7 = 0$

(8 Marks)

c) Given that the matrix A below is singular, find the possible values of  $x$

$$A = \begin{pmatrix} 4 & -1 & 3 \\ x & 2 & 5 \\ 7 & -1 & x \end{pmatrix} \quad (7 \text{ Marks})$$

### Question Three (20 Marks)

a) Obtain the first three non-zero terms of the Maclaurin's series for  $\sin(x)$  hence evaluate

$$\int_0^1 \frac{\sin(x)}{\sqrt{x}} dx \quad (10 \text{ Marks})$$

b) Given that  $\cos(45^\circ) = \sin(45^\circ) = \frac{1}{\sqrt{2}}$ , use the first three terms of a suitable Taylor's series to find the value of  $\cos(44^\circ)$  correct to 4 decimal places. (10 Marks)

### Question Four (20 Marks)

a) Find the inverse of the matrix

$$A = \begin{pmatrix} 1 & 4 & -1 \\ -7 & 2 & 3 \\ 8 & -5 & 9 \end{pmatrix} \quad (9 \text{ Marks})$$

b) Use Cramer's rule to find the solution to the linear system of equations

$$x - 2y + 3z = -11$$

$$3x + y - 2z = 10$$

$$4x - 3y - 5z = 5$$

(11 Marks)

### Question Five (20 Marks)

a) Given that  $Me^x + Ne^{-x} = 2\cosh(x) + 5\sinh(x)$  for all values of  $x$ . Determine the values of  $M$  and  $N$  (4 Marks)

b) Prove that  $\coth^{-1}(x) = \frac{1}{2} \ln \left| \frac{x+1}{x-1} \right|$  for  $|x| > 1$   
hence find the value of  $\coth^{-1}(1.2)$  (7 Marks)

c) Solve the equation  $3\cosh(2x) - \sinh(x) = 1$  (9 Marks)